# Computational minimization of over-deposition at corners of trajectories in Laser Metal Deposition 

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#### Abstract

Avoidance of over-deposition at trajectory corners is relevant in Laser Metal Deposition (LMD) for Additive Manufacturing. Currently available LMD hardware only allows constant material feed (g/s). Therefore, gliding speed of the material dispenser is the remaining tuning variable for controlling metal over-deposition at corners. Existing literature reports trial-error physical experiments, addressing only particular corner angles. In response, this manuscript reports the implementation of a voxel-based simulator of the bead geometry, taking into consideration bead profile, dispenser velocity, material feed, and bead curve geometry. We use it to evaluate two constant-feed tailored-velocity strategies for minimizing material over-deposition at corners.


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## 1. Introduction

Laser Metal Deposition (LMD) employs a laser beam to melt a jet of metal powder and to deliver it onto a workpiece. This promising Additive Manufacturing (AM) technique is used in workpiece coating, repairing and re-manufacturing [1,2]. However, over-deposition of metal on curved or sharp-corner beads is a standing challenge for LMD.

In this manuscript, we present the implementation of a voxelbased simulator of the bead geometry, taking into consideration bead cross profile, nozzle velocity, variable material feed, and bead curve geometry. Our simulator allows for time-varying material feed (g/s), although this feature is an open research topic at the present time. We couple our bead geometry simulator with two variable speed strategies, used to minimize material overdeposition in corners.

## 2. Literature review

AM uses Piecewise Linear (PL) trajectories. Two factors reinforce metal over deposition at corners: (i) overlapping deposition zone (Fig. 1(a)) and (ii) nozzle deceleration. The proposed methods in

[^0]the literature to reduce over-deposition at the corners are (1) the control of the process parameters (e.g. speed, power and material flow) [3], (2) corner smoothing [4-6] and (3) a combination [7,8] of (1) and (2). Corner smoothing is only acceptable if accuracy is not a priority. The authors [3] that aim only to control the process parameters (e.g. speed, power, material flow) do not use numerical methods to study the influence of the parameters in the corner deposition. Instead, they employ costly physical trial-error experimentation and limit their studies to right ( $90^{\circ}$ ) angles.

We identified two approaches to model computationally the bead geometry in LMD. The first assumes a pre-defined bead cross-section, namely circular [9-12], elliptical [9,13], parabolic [9,11,12,14,15], sinusoidal [9,11,12]. Other researchers [16,3] model bead width and height as functions of process parameters.

In the second method, the bead geometry is not pre-defined but it is induced by the distribution of the delivered material which depends on the process parameters [17,10,18,19]. We consider that, under conditions of full melting of the powder jet, the variation in nozzle velocity or material feed are more immediate factors to control over-deposition. Mainly two types of delivered material functions have been studied: Gaussian [17,10,18,19] and uniform [10]. Our simulator accepts any material distribution function $f: \mathbb{R}^{2} \rightarrow \mathbb{R}$.


Fig. 1. Trajectory corner. Parameters, goal bead and discretization.

### 2.1. Conclusions of the literature review

In the existing literature, sharp corners deposition in LMD is addressed by smoothing the corner geometry and expensive trial-and-error experimentation. This manuscript presents an implementation of a material deposition geometric simulator which considers: bead geometry induced by models of delivered material distribution, PL trajectories, nozzle velocity ( $\mathrm{mm} / \mathrm{s}$ ) and feed rate ( $\mathrm{g} / \mathrm{s}$ ).

## 3. Methodology

### 3.1. Geometry deposition model

### 3.1.1. Powder delivery density

The function $I(x, y, t)\left(\mathrm{g} /\left(\mathrm{smm}^{2}\right)\right)$ reflects, given a time $t$, the metal particle density projected by the nozzle at the workpiece surface. Coordinate $z$ is parallel to the jet. Eq. 1 represents a Gaussian example of this distribution, with coordinates $(x, y)$ already measured on the workpiece surface. Our simulator accepts any density function of $(x, y)$ :
$I(x, y, t)=\frac{2 f(t)}{\pi R^{2}} \exp \left(\frac{-2\left(\left(x-P_{x}(t)\right)^{2}+\left(y-P_{y}(t)\right)^{2}\right)}{R^{2}}\right)$.
$f$ is the material feed rate $(\mathrm{g} / \mathrm{s}), R$ is half of the nominal bead width (mm), $\boldsymbol{P}(t)=\left[P_{x}(t), P_{y}(t)\right]^{T}$ is the nozzle position (mm, mm) at time $t$.

Given the function I, the material density $\rho$ and the total deposition time $T$, one can obtain the bead height $H$ as:
$H(x, y)=\frac{1}{\rho} \int_{0}^{T} I(x, y, \xi) d \xi$.

### 3.1.2. Nozzle trajectory

$C=[p 0, . ., p N]$ is a PL approximation of the nozzle trajectory. $f_{k}$ and $v_{k}$ are the feed and velocity levels at point $\boldsymbol{p}_{k}$. Acceleration is assumed constant when velocity changes. Let $t_{k}(0 \leqslant k \leqslant N)$ be the time at which the dispenser reaches point $\boldsymbol{p}_{k}$, with $t_{0}=0$ and $t_{N}=T$. Each $t_{k}$ is a function of the speeds $v_{0}, v_{1}, \ldots, v_{k}$. We numerically compute the bead height as per Eq. (3):
$H(x, y)=\frac{1}{\rho} \sum_{k=1}^{N} \int_{t_{k-1}}^{t_{k}} I(x, y, \xi) d \xi$.

### 3.2. Minimization of material overfill in corners

We define an ideal corner as the one in which incoming and outgoing beads are free from over- and under-deposition. The ideal
bead profile $H_{0}$ in Eq. (4) corresponds to the steady state in a linear nozzle trajectory. For the purpose of computing $H_{0}$, we may consider this trajectory on the $X$ axis and therefore $H_{0}(x, y)=H_{0}(y)$.
$H_{0}(x, y)=\int_{-\infty}^{\infty} I(x, y, t) d t=\frac{\sqrt{2} f}{\rho \sqrt{\pi} R v} \exp \left(\frac{-2 y^{2}}{R^{2}}\right)$.
The ideal or goal corner corresponds to an assembly of incoming and outgoing beads. They are completely symmetrical w.r.t. a plane bisecting the corner angle (Fig. 1).

Considerations for corners in LMD are: (a) Over-deposition is reinforced by (i) overlapping zones in incoming and outgoing beads (Fig. 1), ii) mandatory deceleration to reach null velocity at the corner itself. (b) Current LMD hardware is unable to produce variable feed ( $\mathrm{g} / \mathrm{s}$ ) within the trajectory [20,21,3], leading to an overall constant feed. Because of these considerations, we proceed to use the nozzle cruise velocity as variable to minimize material over-deposition at corners.

The tuning variables for the over-deposition minimization are the nozzle speeds $V=\left(v_{0}, \ldots, v_{N}\right)$ at each vertex $\boldsymbol{p}_{k}$ of the corner discretization. We define the optimization problem assuming the domain is discretized into a rectangular grid $G$ with vertices $\left(x_{i}, y_{j}\right),\left(1 \leqslant i \leqslant G_{1}, 1 \leqslant j \leqslant G_{2}\right)$, as shown in Fig. 1(c). The optimization problem is stated as follows:

$$
\text { find } \quad V=\left(v_{0}, \ldots, v_{N}\right)
$$

to minimize

$$
E_{k}(V)=\frac{1}{G_{1} G_{2}} \sum_{i=1}^{G_{1}} \sum_{j=1}^{G_{2}} e_{k}\left(x_{i}, y_{j}\right)^{2}
$$

subject to

$$
\begin{gather*}
0 \leqslant v_{i} \leqslant v_{\max }, \quad i=0,1, \ldots, N  \tag{5}\\
\|\boldsymbol{a}(t)\| \leqslant a_{\max }, \quad t \in[0, T]
\end{gather*}
$$

$\boldsymbol{a}(t)=\left[a_{x}(t), a_{y}(t)\right]^{T}$ is the nozzle acceleration. $v_{\text {max }}$ and $a_{\text {max }}$ are the maximal speed and acceleration permissible for the AM hardware or the process, respectively. $e_{k}: \mathbb{R}^{2} \rightarrow \mathbb{R}$ is an error function that measures the deviation of the actual (given the speeds $V$ ) height w.r.t. the goal height. We consider two error functions:

1. Direct comparison between the actual and the goal height:

$$
\begin{equation*}
e_{1}(\mathbf{x})=\left|H(\mathbf{x})-H_{G}^{\theta}(\mathbf{x})\right| \tag{6}
\end{equation*}
$$

2. A more permissive function to diminish underfill due to nozzle acceleration:

$$
e_{2}(\mathbf{x})=\left\{\begin{array}{cc}
\left|H(\mathbf{x})-H_{G}^{\theta}(\mathbf{x})\right|, & H(\mathbf{x})<H_{G}^{\theta}(\mathbf{x}), \text { i.e. underfill }  \tag{7}\\
0, & H_{G}^{\theta}(\mathbf{x}) \leqslant H(\mathbf{x}) \leqslant \max \left(H_{G}^{\theta}\right), \\
& \text { i.e. permissible overfill } \\
H(\mathbf{x})-\max \left(H_{G}^{\theta}\right), & H(\mathbf{x})>\max \left(H_{G}^{\theta}\right), \text { i.e. overfill }
\end{array}\right.
$$

where $\max \left(H_{G}^{\theta}\right)=H_{0}(x, 0)=\frac{\sqrt{2} f}{\rho \sqrt{\pi} R \nu}$.

## 4. Results

For the purpose of illustration, we produce the results of minimizing over-deposition with corner angles $\theta \in\left\{30^{\circ}, 60^{\circ}, 90^{\circ}\right\}$ and
Table 1
Simulation set-up. Parameters for the optimization of material overfill at the corners deposition. Values based on Refs. [20,22,23].

| Parameter | Value |
| :--- | :--- |
| Material | AISI 316 L |
| Density | $\rho=7900 \mathrm{~kg} / \mathrm{m}^{3}[23]$ |
| Clad radius | $R=2.3 \mathrm{~mm}$ |
| Nozzle cruising speed | $v_{c}=13 \mathrm{~mm} / \mathrm{s}$ |
| Material feed rate | $f=0.42 \mathrm{~g} / \mathrm{s}$ |
| Maximal speed | $v_{\max }=2 v_{c}=26 \mathrm{~mm} / \mathrm{s}$ |
| Maximal acceleration | $a_{\max }=600 \mathrm{~mm} / \mathrm{s}^{2}[20]$ |

use the conditions of Table 1. The material properties specific for LMD used in the simulation correspond to AISI 316L stainless steel in [22].

Our model parametrizes the magnitude of the dispenser cruise speed in terms of the distance $d$ from the corner tip. We approximate the optimal speed function $V^{0}$ by a 4 -stage PL function (see Table 2). The stages of $V^{0}$ are nonlinear functions of $d$. Given consecutive checkpoints $\left(d_{i}, v_{i}\right)$ and $\left(d_{i+1}, v_{i+1}\right)$ the velocity between them is given by:
$V^{0}(d)=\sqrt{2 a\left(d-d_{i}\right)+v_{i}^{2}}, \quad d \in\left[d_{i}, d_{i+1}\right]$,
where $a$ is the constant acceleration in the stage.
The minimization uses the exhaustive search method to find the optimal velocity histories for error accountancy methods $e_{1}$ and $e_{2}$. This method is expensive in computing time. Therefore, this

Table 2
Row 1: Optimal speed profiles $V_{e_{1}}^{0}, V_{e_{2}}^{0}$ for errors $e_{1}$ and $e_{2}$. Corner angles $\theta \in\left\{30^{\circ}, 60^{\circ}, 90^{\circ}\right\}$. Rows 2-6: Resulting bead geometries. Row 2: no velocity control. Rows 3-4: Beads with optimal velocity, given errors $e_{1}$ and $e_{2}$, respectively. Rows 5-6: Bead cross-section $Y=0$ with optimal velocity, given errors $e_{1}$ and $e_{2}$, respectively.



Fig. 2. Over-deposition consolidated estimators $E_{1}$ and $E_{2}$ (Eq. (5)) for velocity profiles $\left\{V_{v_{c}}, V_{e_{1}}^{0}, V_{e_{2}}^{0}\right\}$ and corner angles $\left\{30^{\circ}, 60^{\circ}, 90^{\circ}\right\}$. $e_{1}$ and $e_{2}$ : deposition punctual error methods (Eqs. (6) and (7), respectively).
optimization is to be used at the stage of process-planning and not in real time during the manufacturing itself. The resulting speed profiles for each studied value of the corner angle $\theta$ are presented in Table 2. For each angle, we found speed profiles $V_{e_{1}}^{0}$ and $V_{e_{2}}^{0}$ as per the error $e_{1}$ and $e_{2}$ functions in Eqs. (6) and (7).

The (decreasing) distance to the next corner presents velocity plots which occur in the negative horizontal axis. However, notice that the entry and exit velocity histories are, under the current assumptions, symmetrical with respect to the distance to the corner spot. These considerations lead to Table 2 presenting the dispenser velocity at the exit from the corner and not in the entry phase. Both, $V_{e_{1}}^{0}$ and $V_{e_{2}}^{0}$ show similar behavior: (a) large acceleration near the corner, reaching the maximal value $v_{\text {max }}$, (b) constant speed, and (c) deceleration to reach the cruise speed $v_{c}$. The sharper the corner, the smaller the angle $\theta$ and (as expected) the more abrupt the acceleration or deceleration near the corner spot. Error accountancy methods $e_{1}$ and $e_{2}$ call for the same acceleration (or deceleration) to depart from (or reach to) null velocity at the corner. However, the transition to cruise speed takes longer with method $e_{1}$. Therefore, the average speed of $V_{e_{1}}^{0}$ is greater than the one of $V_{e_{2}}^{0}$.

Table 2 shows the height functions for $\theta \in\left\{30^{\circ}, 60^{\circ}, 90^{\circ}\right\}$ associated to (1) the optimal speed functions $V_{e_{i}}^{0}(i=1,2)$ and (2) a simulation with a constant speed function $V_{v_{c}}$ (which would require infinite acceleration/deceleration at the corner spot).

In Table 2, (1) we can observe the material over-deposition at constant speed $V_{v_{c}}$ is evident for all $\theta \in\left\{30^{\circ}, 60^{\circ}, 90^{\circ}\right\}$. Additionally, over-deposition increases when the angle decreases. (2) In the cross-section views for $\theta=30^{\circ}$, we can note that $V_{e_{1}}^{0}$ produces more underfill than $V_{e_{2}}^{0}$. Since the average speed of $V_{e_{1}}^{0}$ is greater than the one of $V_{e_{2}}^{0}$, the amount of deposited material is lower.

The values of the objective functions (i.e. sum of squared errors in Eq. (5)) for the optimal velocity functions $V_{e_{1}}^{0}$ and $V_{e_{2}}^{0}$, and for the constant (uncontrolled) velocity function $V_{v_{c}}$ are depicted in Fig. 2. The difference of the objective functions between the optimal ( $V_{e_{1}}^{0}, V_{e_{2}}^{0}$ ) and uncontrolled ( $V_{v_{c}}$ ) velocity functions is noticeable. The values under uncontrolled speed are at least 10 times greater than for the optimal solutions $\left(E_{i}\left(V_{v_{c}}\right) / E_{i}\left(V_{e_{i}}^{0}\right)>10, i=1,2\right)$. We can also observe that, for every value of $\theta \in\left\{30^{\circ}, 60^{\circ}, 90^{\circ}\right\}$, the minimal value of $E_{1}$ is attained by $V_{e_{1}}^{0}$ (analogously for $E_{2}$ and $V_{e_{2}}^{0}$ ).

## 5. Conclusions

In this manuscript, we have presented the implementation of a voxel-based geometric simulator for Laser Metal Deposition (LMD).

On this simulator, we have mounted and solved a minimization of the material over-deposition at corners in LMD. Results for the corner angle instances $\theta \in\left\{30^{\circ}, 60^{\circ}, 90^{\circ}\right\}$ show a reduction of over $90 \%$ of the over-deposition present at corners with no nozzle velocity control. An exhaustive search strategy is used for minimization. This strategy is expensive in computing time. Therefore, our method is to be used for the process planning stage. Further study of heuristics for cutting computing time expenditures are required for in-process applications.

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## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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